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# **An Empirical Analysis of the Mean-Reversion Property of Real Interest Rates**

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## **Abstract**

This paper examines the mean-reversion property of real interest rates of a number of industrialized and East Asian countries. Many past studies have found the evidence of mean-aversion, which has been a puzzling outcome. We have employed panel unit root tests and half-life estimation based on the bias-corrected bootstrap, which allow for the presence of cross-sectional dependence. We have found that the real interest rates are overall mean-reverting. It is also found that the real interest rates of industrialized countries show a lower rate of mean-reversion than those of East Asian markets. For East Asian emerging markets, we have found evidence that the speed of mean-reversion has become slower after the Asian crisis. Our results strongly suggest that the speed of mean-reversion is closely related with the degree of market friction caused by government interventions. There is a strong tendency that the rates form more advanced and liberalized markets show slower speed of mean-reversion.

**Keywords: Bootstrap, Cross-sectional dependence, Half-life, Highest Density Region, Panel unit root tests, Stationarity.**

**JEL Classifications: F21, G15, C63**

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## 1. Introduction

The real interest rate, the nominal interest rate adjusted with inflation, represents the growth rate of purchasing power derived from an investment. It plays a crucial role in a wide range of prominent economics and finance models, including the neoclassical growth models (Solow, 1956), Black-Scholes option pricing model (Black and Scholes, 1973), consumption-based capital asset pricing models (Lucas, 1978; and Hansen and Singleton, 1982), and Fisher equation (Fisher, 1930). These models assume that, *ceteris paribus*, the real interest rate is constant over time. For example, the Fisher equation postulates that a rise in (expected) inflation rate will eventually cause an equal rise in the nominal interest rate. This indicates that, in practice, the real interest rate should be mean-reverting or stationary, where a deviation from its long run level has only a transitory effect.

The accumulated empirical evidence on the time series properties of real interest rate, however, has provided rather mixed and puzzling outcomes. Most past studies tested stationarity or otherwise of real interest rate using (univariate) unit root tests. Using annual and monthly US data, Rose (1988) found that the nominal interest rate is  $I(1)$  while inflation rate is  $I(0)$ , and that real interest rate is  $I(1)$ .<sup>1</sup> Rapach and Weber (2004), using quarterly data for 16 industrialized countries, found that both nominal interest and inflation rates are  $I(1)$ . This result implies

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<sup>1</sup> A time series with a unit root is non-stationary and exhibit a mean-averting behavior over time with a shock to the time series having a permanent effect. Such a time series is said to be integrated of order 1, denoted as  $I(1)$ . A stationary  $I(0)$  time series with no unit roots shows mean-reverting behavior, where the time series shows a strong tendency to revert back to its long-run mean after a shock is given.

that the Fisher equation represents a spurious relationship between the nominal interest rate and inflation. On the other hand, Lai (2004, 2008) provided evidence that real interest rates are mean-reverting for a number of industrialized and developing countries, based on the univariate unit root tests with mean-shift alternatives. In contrast, Phillips (2005) examined the long memory property of real interest rate using US historical data, and concluded that it is fractionally non-stationary, i.e., it is of  $I(d)$  with  $0.5 \leq d < 1$ .

Rapach and Wohar (2004) took a different approach by calculating the half-life of real interest rates. The half-life is a popular measure of mean-reversion, defined as the number of periods (or years) required for the response of a time series to a unit shock to dissipate by one half. It has been used widely in international economics to test for the empirical validity of parity conditions such as the purchasing power parity (see, for example, Rogoff; 1996). The half-life of an  $I(0)$  time series is positive and finite, while that of an  $I(1)$  time series is infinite. Rapach and Wohar (2004) constructed confidence intervals for the half-life of real interest rates based on the grid bootstrap of Hansen (1999), which is a method applicable to a univariate time series. These authors found that the intervals for all 13 countries have infinite upper bounds. This indicates that the real interest rates are not statistically distinguishable from an  $I(1)$  time series, which is evidence of mean-reversion.

When this discussion reaches the equity premium puzzle and the risk free rate

puzzle, spurred by Mehra and Prescott (1985) and Weil (1989), stationarity of real interest rate faces an even bigger challenge. Explanation of these puzzles has become one of the central issues in macroeconomics and finance, and continuing research efforts are being devoted to it up to date. This stream of literature found equity returns to be mean-reverting, while real interest rate mean-averting. For instance, Fama and French (1988) and Poterba and Summers (1988) found negative auto-correlation in equity returns over long horizons. Siegel and Thaler (1997) quoted these findings to suggest that the equity premium puzzle is even more challenging than what had been previously thought because not only the size of the equity premium but also now its sign is a mystery: “It is not that the risk of equities is not great enough to explain their high rate of return; rather, for long-term investors, fixed income securities have been riskier in real terms. By this reasoning, the equity premium should be negative!”

In this paper, we re-examine the mean-reversion property of real interest rates for a number of industrialized and East Asian countries. The former represent highly liberalized capital markets; while the latter a mixture of liberalized markets and emerging markets. For the former, we examine tax-adjusted quarterly real bond yield from thirteen countries, previously investigated by Rapach and Wohar (2004). For the latter, we use short-term monthly real interest rates of seven East Asian capital markets, paying attention to the effect of the Asian currency crisis in 1997, which exerted considerable impact on most of capital markets in this region. In the methodological content, this paper is distinct from the past studies on two

points. First, we combine the results from panel unit root testing and half-life estimation in this paper. Second, our testing and estimation methods take account of cross-sectional dependence among the real interest rates, which is a point totally overlooked by the above-mentioned past studies.<sup>2</sup>

We use the panel unit root (IPS) test developed by Im et al. (2003) and the inverse normal test of Choi (2001) to test whether a set of real interest rates are stationary. We consider the subsampling versions of these tests proposed by Choi and Chue (2007), which allow for cross-sectional dependence of the time series in the panel. We conduct half-life estimation based on the bias-corrected bootstrap, recently proposed by Kim et al. (2007), where the highest density region (HDR) method of Hyndman (1996) is used to construct confidence intervals. This HDR method provides a more sensible way of constructing confidence intervals for half-life than the conventional methods, given the atypical distributional properties of the half-life estimator. Kim et al. (2007) provided Monte Carlo evidence that their bias-corrected bootstrap HDR method performs much better than the conventional methods in small samples. In this paper, we extend the methods of Kim et al. (2007), so that the half-life estimates are calculated using a vector autoregression, in order to take explicit account of cross-sectional dependence of the time series.

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<sup>2</sup> There has been voluminous literature on real interest linkages across international capital markets (see, for example, Chin and Frankel, 1995, Glick and Hutchison, 1990; Goldberg et al, 2003; Goodwin and Grennes, 1994; Phylaktis, 1999). Current standing on the degree of real interest linkages in the literature is that high income countries such as European markets and the US appear to be integrated more than Asian markets in the context of cointegration, although there is little empirical support for real rate equalisation. For East Asian countries, Phylaktis (1999) found evidence to suggest that financial liberalisation increased integration.

The main finding of the paper is that international real interest rates are mean-reverting for both industrialized and East Asian countries. We have found that the East Asian real interest rates overall show a faster convergence to long-run mean than those of industrialized countries. For the East Asian emerging markets in particular (excluding Japan and Singapore), we have found evidence that the speed of mean-reversion has become substantially lower after the crisis. These results suggest that the markets with a higher degree of market friction caused by government interventions show faster mean-reversion of the real interest rates. In the next section, we present the details of the methodologies used in this study. Section 3 provides the data details, and Section 4 provides the empirical results. Section 5 concludes the paper.

## **2. Methodologies**

An attraction of panel unit root testing is that, by pooling the observations from different cross-sectional units, the test can enjoy a larger sample size, which can give rise to a higher power. However, as Maddala and Kim (1998; p.138) noted, it may be of limited value in practice because it does not reveal the speed of convergence or mean-reversion associated with individual time series. To measure the speed of mean-reversion, the half-life is also estimated in this paper.

### **2.1. Panel Unit Root tests**

#### **Im-Pesaran-Shin (IPS) test**

Im et al. (2003) considered a model of the form

$$\Delta Y_{it} = \mu_i + \phi_i Y_{it-1} + \sum_{j=1}^{p_i} \phi_{ij} \Delta Y_{it-j} + e_{it}, \quad (1)$$

where  $i$  ( $= 1, \dots, N$ ) indicates a cross-sectional unit,  $t$  ( $= 1, \dots, T$ ) is a time index and  $e_{it} \sim \text{IID}(0, \sigma^2)$ . They specified the null and alternative hypotheses of the form

$$\begin{aligned} H_0 : \phi_1 = \phi_2 = \dots = \phi_N = 0 \\ H_1 : \phi_1 < 0, \phi_2 < 0, \dots, \phi_{N_0} < 0 \quad (N_0 \leq N) \end{aligned} \quad (2)$$

The null hypothesis indicates that all time series in each cross-sectional unit are non-stationary with a unit root. Under the alternative hypothesis, at least  $N_0$  time series are stationary. The test statistic is constructed from the t-test statistics calculated from individual cross-sectional units. Let  $\hat{\tau}_i$  denote the augmented Dickey-Fuller (ADF) t-statistic to test for  $\phi_i = 0$ . Im et al. (2003) have shown that

$$\frac{\sqrt{N}(\hat{\tau}_N - E(\hat{\tau}_i))}{\sqrt{\text{Var}(\hat{\tau}_i)}} \Rightarrow N(0,1),$$

where  $\hat{\tau}_N = \frac{1}{N} \sum_{i=1}^N \hat{\tau}_i$ . That is, the average of  $\hat{\tau}_i$  statistics over all cross-sectional units converges to the standard normal distribution, when standardized. The values of  $E(\hat{\tau}_i)$  and  $\text{Var}(\hat{\tau}_i)$  are tabulated in Im et al. (2003).

### **Inverse normal test**

Choi (2001) suggested a test for the null and alternative hypotheses given in (2) based on the p-values of individual statistics. Let  $\pi_i$  denote the p-value of the individual t-statistic  $\hat{\tau}_i$ . Choi (2001) proposed the inverse normal test

$$Z_{NT} = \frac{1}{\sqrt{N}} \sum_{i=1}^N \Phi^{-1}(\pi_i),$$

where  $\Phi(\cdot)$  is the standard normal cumulative distribution function. Under the null hypothesis given in (1), as  $T \rightarrow \infty$ ,  $Z_{NT}$  converges to  $\frac{1}{\sqrt{N}} \sum_{i=1}^N z_i$  where  $z_i$  follows the standard normal distribution.

### **Subsampling for cross-sectional dependence**

The IPS and Fisher ADF tests above assume cross-sectional independence. This can be unrealistic in practice since it is highly likely that the time series in the panel are contemporaneously correlated. That is, the vector of error term  $(e_{1t}, \dots, e_{Nt})$  has the covariance matrix with non-zero off-diagonal elements. To allow for this dependence, Choi and Chue (2007) proposed the subsampling versions of the IPS and Fisher ADF tests. The subsampling method (Romano and Wolf, 2001) approximates the sampling distribution of a statistic, by calculating the test statistic of interest from overlapping subsamples of the observed data.

Let  $Z_t = (Y_{1t}, \dots, Y_{Nt})$  be the vector of panel time series at time  $t$ . Let the subsample of size  $b$  be denoted as  $W_s = (Z_s, Z_{s+1}, \dots, Z_{s+b-1})$  ( $1 \leq s \leq T-b+1$ ). Let  $T$  be the statistic of interest and  $T_s$  be the statistic calculated from the subsample  $W_s$ . Calculate the statistic for all possible subsamples give the collection of the statistics  $\{T_s\}_{s=1}^{T-b+1}$ , which can be used as an approximation to the sampling distribution of  $T$ . Since a subsample preserves cross-sectional dependence,  $\{T_s\}_{s=1}^{T-b+1}$  provides a small sample distribution of  $T$ , allowing for cross-sectional dependency. Choi and Chue (2007) proposed the subsampling versions of IPS and

Fisher ADF tests. They showed that, under certain regularity conditions, these subsampling tests are consistent and possess valid asymptotic properties (Choi and Chue, 2007; Theorems 1 and 2). To implement the tests for the null hypothesis given in (2), we use the critical values obtained from  $\{T_s\}_{s=1}^{T-b+1}$ .

In implementing the subsampling tests, the choice of the subsample length  $b$  is important. Choi and Chue (2007) proposed two data-dependent methods: one based on simulation-based calibration rule and the other on minimum volatility rule. Both methods are used in this paper, although their details are not given here for simplicity.

## **2.2 Half-life estimation**

The half-life is widely used as a measure of persistence or mean-reversion of economic time series, particularly in the context of testing for the validity of parity conditions in international economics. For example, mean-reversion of real exchange rates is a key condition for the empirical validity of purchasing power parity (Rogoff, 1996). In the simple case of the univariate AR(1) model, the half-life is calculated as  $\log(0.5)/\log(\alpha)$ , where  $\alpha$  is the AR(1) slope coefficient. In the higher order or higher dimensional case, a closed form solution does not exist, but the half-life can be calculated from the impulse response function.

In this paper, we calculate point and interval estimates of half-life using the bias-corrected bootstrap proposed by Kim et al. (2007), who reported Monte Carlo

evidence that their method performs substantially better than the existing methods of half-life estimation. We extend their bias-corrected bootstrap based on the univariate AR model to the vector autoregression (VAR), and estimate the half-life of a time series taking account of cross-sectional dependence.

### VAR model and estimation

We consider the  $N$ -dimensional vector autoregressive (VAR) model of the form

$$Z_t = \nu + B_1 Z_{t-1} + \dots + B_p Z_{t-p} + u_t, \quad (3)$$

where  $Z_t = (Y_{1t}, \dots, Y_{Nt})$  is the  $N \times 1$  vector of variables at time  $t$ ,  $\nu$  is the  $N \times 1$  vector of intercepts, and  $B_i$ 's are the  $N \times N$  matrices of coefficients. Note that  $u_t$  is the  $N \times 1$  vector of innovations with  $E(u_t) = 0$  and  $E(u_t u_t') = \Sigma_u$ . The unknown VAR order  $p$  in (1) is estimated using the Bayesian information criterion (BIC).

The impulse responses are calculated from the coefficients of the  $MA(\infty)$  representation of the VAR model. Given  $T$  realizations  $(Z_1, \dots, Z_T)$  of (2), the unknown coefficients are estimated using the least-squares (LS) method. The LS estimators for  $B = (\nu, B_1, \dots, B_p)$  is denoted as  $\hat{B} = (\hat{\nu}, \hat{B}_1, \dots, \hat{B}_p)$ , and the associated vector of residuals as  $\{\hat{u}_t\}_{t=p+1}^n$ . The impulse responses are defined as  $\Phi_i$  where  $\Phi_i$ 's are the coefficients of the  $MA(\infty)$  representation of (1). A typical element of  $\Phi_i$  is denoted as  $\theta_{kl,i}$ , and it is interpreted as the response of the variable  $k$  to a one-time impulse in variable  $l$ ,  $i$  periods ago. The plot of  $\theta_{kl,i}$  against  $i$  is called the impulse response function of the variable  $k$  to a one-time

impulse in variable  $l$ . Using  $\hat{B}$ , the estimator for impulse response  $\hat{\theta}_{kl,i}$  for  $\theta_{kl,i}$ , can be calculated.

As mentioned earlier, the half-life of a time series is defined as the number of periods required for the response of a time series, to its own shock, to be halved. As such, it can readily be obtained from the impulse response function of a time series. In the VAR case, the half-life of the  $k^{\text{th}}$  time series in the system, denoted as  $h_k$  can be calculated from the impulse response function to its own shock, namely  $\theta_{kk,i}$ , where  $k = 1, \dots, K$ . The half-life estimator for  $h_k$ ,  $\hat{h}_k$ , can be obtained from  $\hat{\theta}_{kk,i}$ .

### **Bias-corrected bootstrap for point and interval estimation**

The bootstrap is a computer-intensive method of approximating the sampling distribution of a statistic. It has been applied widely in econometrics and is often found to provide a superior alternative to the conventional methods in small samples (see, Li and Maddala, 1996; Berkowitz and Kilian, 2000; and MacKinnon, 2002). Note that impulse response estimates and half-life estimates are necessarily biased in small samples, due to small sample biases present in the VAR parameter estimators (see Tjostheim and Paulsen, 1983; Nicholls and Pope, 1988; and Pope, 1990). The biases are particularly severe when the VAR model has unit roots or near unit roots; when the VAR dimension  $N$  is larger; or when the sample size is smaller. It is highly likely that these biases adversely affect the small sample properties of the confidence intervals.

To obtain confidence intervals with improved small sample properties, Kilian (1998a, 1998b) proposed the use of the bias-corrected bootstrap (or bootstrap-after-bootstrap). It is a bootstrap method of constructing confidence intervals, in which the biases associated with parameter estimators are adjusted in two stages of the bootstrap. Although it was originally proposed for statistical inference of impulse response, the bias-corrected bootstrap can easily be adapted to half-life estimation. The bias-corrected bootstrap of Kilian (1998a, 1998b) involves two stages of bias-correction for VAR parameter estimates. Here we follow Kilian (1998b) in using Pope's (1990; p.253) asymptotic bias formula to obtain bias-corrected parameter estimators.

The bias-corrected confidence interval for  $\theta_{kl,i}$  can be obtained as below:

In Stage 1, Pope's (1990) formula is applied to  $\hat{B} = (\hat{v}, \hat{B}_1, \dots, \hat{B}_p)$  to obtain the bias-corrected estimator  $\hat{B}^c = (\hat{v}^c, \hat{B}_1^c, \dots, \hat{B}_p^c)$  for  $B$ . It is possible that  $\hat{B}$  satisfies the condition of stationarity, while  $\hat{B}^c$  does not. In this case, Kilian (1998a, 1998b) suggested an adjustment to  $\hat{B}^c$  so that it implies stationarity. This adjustment is called the stationarity correction, and its details can be found in Kilian (1998a, 1998b).

In Stage 2, generate a pseudo data set following the recursion

$$Y_t^* = \hat{\nu}^c + \hat{B}_1^c Y_{t-1}^* + \dots + \hat{B}_p^c Y_{t-p}^* + u_t^*, \quad (3)$$

using the first  $p$  values of the original data as starting values and  $u_t^*$ 's are generated as random resampling of  $\hat{u}_t$ 's with replacement.

In Stage 3, using  $\{Y_t^*\}_{t=1}^n$ , the VAR coefficient matrices are re-estimated and denoted as  $\hat{B}^* = (\hat{\nu}^*, \hat{B}_1^*, \dots, \hat{B}_p^*)$ . Pope's (1990) bias formula is again applied to  $\hat{B}^*$  in order to obtain a bias-corrected version  $\hat{B}^{*c} = (\hat{\nu}^{*c}, \hat{B}_1^{*c}, \dots, \hat{B}_p^{*c})$  of  $\hat{B}^*$ . The stationarity correction is again applied to  $\hat{B}^{*c}$  if necessary.

Repeat Stages 2 and 3 sufficiently many times, say  $m$ , to generate bootstrap replicates of  $\{\hat{B}^{*c}(j)\}_{j=1}^m$ , and the bootstrap replicates of half-life  $\{\hat{h}_k^*(j)\}_{j=1}^m$  are obtained from  $\{\hat{\theta}_{kk,i}^*(j)\}_{j=1}^m$  in Stage 3. The  $100(1-2\alpha)\%$  bias-corrected bootstrap confidence intervals for  $h_k$  can be constructed as the interval  $[\hat{h}_k^*(\alpha), \hat{h}_k^*(1-\alpha)]$ , where  $\hat{h}_k^*(q)$  is the  $q$ th percentile from the distribution of  $m$  bootstrap replicates  $\{\hat{h}_k^*(j)\}_{j=1}^m$ . To obtain a tight and informative confidence interval from  $\{\hat{h}_k^*(j)\}_{j=1}^m$ , we follow Kim et al. (2007) to use the HDR method of Hyndman (1996).<sup>3</sup>

### HDR point and interval estimators for half-life

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<sup>3</sup> Note that we have set  $m = 2000$  throughout the paper.

Let  $f(x)$  be the density function for a random variable  $X$ . The  $100(1-\theta)\%$  HDR is defined (Hyndman, 1996) as the subset  $R(f_\theta)$  of the sample space of  $X$  such that  $R(f_\theta) = \{x: f(x) \geq f_\theta\}$ , where  $f_\theta$  is the largest constant such that  $\Pr[X \in R(f_\theta)] \geq 1 - \theta$ .  $R(f_\theta)$  represents the smallest region with a given probability content. In short, the HDR method produces confidence intervals concentrated around the modes of the distribution. In the present context,  $X$  is the half-life estimator of a time series and its density can be estimated from the bootstrap replicates of the half-life  $\{\hat{h}_k^*(j)\}_{j=1}^m$ . We estimate the density  $f(x)$  using a kernel estimator with the Gaussian kernel, with bandwidth selected using the Sheather-Jones (1991) rule. From the estimated density, the mode of the distribution is used as the bias-corrected point estimator for the half-life, along with the interval concentrated around the mode of the distribution with the probability content  $100(1-\theta)\%$ . In the multi-modal case, the global mode and the associated interval are used as point and interval estimates of half-life.

Examples of the bias-corrected HDR point and interval estimates of the half-life are illustrated in Figure 1, where the density estimates of  $\{\hat{h}_k^*(j)\}_{j=1}^m$  for the Thai real interest for Periods I and II are plotted. Note that X-axis is half-life replicates in years. Both graphs clearly indicate that the sampling distribution of half-life estimates heavily skewed, with extreme values on the right end of the distribution. These features are the reflection of the atypical distributional properties of half-life estimators mentioned earlier. The global mode is the bias-corrected HDR

point estimate, while the horizontal lines corresponding to the  $f_\theta$  values where  $\theta = 0.05$ , and the associated intervals indicate 95% HDR confidence intervals. In Period I, the point estimate of half-life is 0.15 years, and 95% confidence interval is [0.08, 0.27] in years. In Period II, the distribution has much higher variability with higher proportion of extreme values. The point estimate 0.99 in Period II is a lot bigger than in Period I, and 95% confidence interval [0.25, 7.94] is also substantially wider. This indicates that the speed of convergence of Thai real interest rate has become slower after the Asian crisis. We provide more discussions about this point in Section 4.

### 3. Data

We re-evaluate the data set of Rapach and Wohar (2004), which are tax-adjusted real bond yields for 13 industrialized countries (Australia, Belgium, Canada, Denmark, France, Ireland, Italy, the Netherlands, New Zealand, Norway, Switzerland, the UK and the US), quarterly from 1960:4 to 1998:3.<sup>4</sup> For East Asian markets, we have selected short-term real interest rates for Japan, two NIE countries (Singapore and Korea) and four ASEAN members of developing countries (Indonesia, Malaysia, Philippines and Thailand).<sup>5</sup> These countries represent major emerging markets in East Asia, except for Japan which is included as a major player in this region. For East Asian rates, we have used monthly data from 1987:1 to 1996:12 (pre-crisis period; Period I), and from 1999:1 to 2007:05 (post-crisis period; Period II). The starting date reflects the

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<sup>4</sup> Rapach and Wohar (2004) provide more detailed description with the data source.

<sup>5</sup> The choice of country is largely determined by data availability.

timing of deregulation where most Asian countries started to liberate their financial markets. All observations from 1997 and 1998 were excluded to eliminate noisy and unstable observations. Most of East Asian countries hit by the crisis were already in financial distress in the first half of 1997 and they only started to display a sign of recovery in September 1998.

For Japan and Indonesia, we use the call rate, while the interbank rate has been used for Singapore and Malaysia. Money market rate is used for Korea, Thailand and the Philippines. To generate real interest rate, seasonally adjusted ex-post inflation rate is subtracted from short term nominal interest rates. To calculate the rate of inflation, the consumer price index is seasonally adjusted with the X-12 method in Eviews (version 6). All nominal interest rates are then deflated by the ex-post inflation rate in order to produce the ex post real interest rate series. All data are obtained from *International Financial Statistic Database*.

#### **4. Empirical Results and Discussion**

Table 1 reports the panel unit root test results for Rapach-Wohar data. The orders  $p_i$ 's in (1) are selected using BIC, following Choi and Chue (2007). The details of the selected orders are not reported for simplicity. Both IPS and the inverse normal tests reject the null hypothesis of unit root for all capital markets, based on the 5% critical values obtained from the subsampling method. The critical values are not so sensitive to the different methods of subsample length selection. Table 2 reports the IPS and inverse normal tests for the East Asian capital markets.

For both Periods I and II, the two tests reject the null hypothesis of unit root, based on the 5% critical values obtained from subsampling. Again, the critical values are not so sensitive to the different methods of subsample length selection.

The half-life estimates are obtained from VAR model given in (3). The VAR orders are selected using BIC. For the Rapach-Wohar data, 13-dimensional VAR(1); while, for the East Asian data, 7-dimensional VAR models are fitted for both Period I and II. Table 3 reports the case for the 13 developed capital markets. The grid bootstrap estimates of Rapach and Wohar (2004) are reproduced from their Table 1. The HDR point estimates are overall smaller than the grid bootstrap estimates: the former have the mean value of 0.97, while the latter 3.47. As for the interval estimates, the grid bootstrap intervals have infinite upper bounds for all markets, indicative of unit-root property of the real interest rates. In stark contrast, the bootstrap bias-corrected HDR interval estimates are tight with finite upper bounds. The mean values of the lower and upper bounds of the bootstrap bias-corrected HDR 95% confidence intervals are [0.44, 7.28], indicating that, on average, the half-life of real interest rates is between 0.44 and 7.28 years with 95% confidence. The main cause of this dramatic difference is our method of half-life estimation, which is different from that of Rapach and Wohar (2004) in the treatment of cross-sectional dependence and construction of bootstrap confidence intervals.

For East Asia, in Period I, the point estimates are in the range of 0.07 to 0.92 years with the mean value of 0.36 years. The 95% confidence intervals are tight, indicating that all rates are mean-reverting. The mean values of the lower and upper bounds of the 95% confidence intervals are 0.13 and 2.41. In Period II, similarly to Period I, all rates show small point estimates and tight confidence intervals. Overall, mean-reversion has become only slightly slower for most countries after the Asian crisis: the mean point estimate of 0.39 years in Period II is nearly same as that of Period I, but the 95% confidence intervals in Period II have median lower and upper bounds of 0.14 and 2.89, which are wider than those of Period I which are 0.14 and 0.89.

### **Speed of Convergence, Financial Frictions, and Risk Premia**

A notable observation from the results presented above is the difference in half-life estimates among capital markets in differing stages of maturity. For the thirteen industrialized countries, the mean point estimate is 0.68 with the mean 95% confidence interval of [0.44, 7.28]. In contrast, as mentioned above, the mean point estimate of the East Asian markets is 0.36 with the mean 95% confidence interval of [0.13, 2.41] before the Asian crisis; the mean point estimate 0.39 with the mean confidence interval of [0.14, 2.89] after the crisis.<sup>6</sup> This indicates that real interest rates for industrialized countries overall show slower

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<sup>6</sup> We have measured univariate half-life but the results are omitted to conserve space. Multivariate half-life estimates are remarkably smaller than univariate for industrialized countries. For East Asian countries the difference between univariate and multivariate estimates is not as dramatic and reserves interpretation. Given the existing evidence on real interest rate linkages in major financial markets, it seems that the interdependence across industrialized countries is captured in the difference between multivariate half-life and univariate estimates. In this sense multivariate half-life estimates provide more accurate measures for speed of convergence for western economies.

convergence than those for East Asian markets. This suggests a tendency that the real interest rates of more matured and liberalized markets show lower degree of mean-reversion.

Our conjecture for a possible cause of such tendency is financial frictions caused by government interventions. It has been long and well documented that East Asian markets experienced a high degree and a large scope of government interventions (see Masuyama et al, 1999). The effects of the intervention on the market still remain as a long-standing issue especially in relation to the East Asian financial crisis (see, for details, Corsetti, Pesenti and Roubini, 1998a, 1998b; and Wade, 1998a, 1998b). A plausible form of financial frictions for East Asian capital markets is financial repressions which include government controls on interest rates, entry, credit allocation, foreign exchange and taxation.<sup>7</sup> Differing views to the effects of financial repressions have been proposed since 1970s. The McKinnon-Shaw approach suggested that financial repression inhibits financial development, while Stiglitz (1994) and Amsden (1989, 2001) argued that some departures from strict market-oriented credit allocation were beneficial (see McKinnon, 1973; Shaw, 1973; Kapur, 1976; Fry, 1978).

Regardless of pros and cons of financial repression as a policy debate, the half-life estimates presented in this paper seem closely related to the degree of the financial friction for East Asia. Relatively large half-life estimates for liberalised markets in

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<sup>7</sup> These restrictions continued to influence the markets mostly heavily at least until the early 1990s. See, for details, Greenwood (1986).

the Rapach-Wohar data imply that market forces drive real interest rates to the long-run mean level at a slower pace. The estimates for the East Asian markets are much smaller, which suggests that the rates deviate in a narrower range due to the financial repression.

The financial crisis dichotomy in mean-reversion for the East Asian markets provide stronger support for our conjecture in relation to the presence of financial friction in these markets when only emerging markets are considered. Excluding the two highly liberated markets, Japan and Singapore<sup>8</sup>, the other members of the East Asian countries show pre-crisis mean half-life of 0.25, with 95% mean interval of [0.11, 1.18]. In the post-crisis period, however, their half-life estimates are much larger overall, with mean point estimate 0.43 with the 95% mean confidence interval of [0.15, 3.54]. We argue that the lower speed of mean-reversion in the post-crisis period is largely due to heavy deregulation-oriented remedy that East Asian emerging markets have commonly implemented. Korea, Indonesia, the Philippines and Thailand adopted either floating or managed floating exchange rate regime and drastically abolished capital controls over the crisis. In particular, Korea, Indonesia, the Philippines and Thailand were the major recipients of the IMF bailout packages with obligations to accept the IMF recommendations for structural reforms, and monetary and fiscal policies.<sup>9</sup> A key post-crisis change that these countries had to accommodate is the removal of

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<sup>8</sup> Although it is difficult to make an exact list of emerging financial markets, market indices such as Morgan Stanley Emerging Markets Index include Korea, Malaysia, Philippines and Thailand as emerging markets. We follow this convention in the paper.

<sup>9</sup> Unlike the others who received support loan package, the Philippines was approved a major extension of existing credit.

control on foreign capital as part of market liberalisation. Our reasoning is that such market deregulation contributes to a decrease in the speed of mean-reversion of real interest rates. If markets are deregulated and unleashed from regulatory monetary authorities, external shocks caused by market forces to data generating process should drive the rates to larger deviations from and slower adjustments to their long-run levels than in a regulated environment. This is evidenced by the fact that half-life point estimates for these recipient countries have all increased over the crisis, with an exception of Indonesia. On the contrary, the point estimate for Malaysia, that refused the IMF intervention, has declined by almost half.

The lower rate of mean-reversion implies that real return from fixed income investment has a larger degree of unpredictable component, and that the investors may be subject to a higher degree of risk, particularly in the long term. Another inference that can be made from the comparison of half-life estimates between the industrialized and East Asian countries is that the participants in less repressed industrialized markets are taking larger risk premium on risk-free assets. A similar finding has been documented in Campbell and Viceira (2002, p78) on US real interest rates, who measured the degree of persistence for real interest rates and inflation and found that, since the early 1980s, aggressive monetary controls on inflation raised risk premia and volatility of returns on fixed income assets. Why long-horizon investors are willing to take such premium in developed countries is another interesting food for thoughts but left as a future research work.

## **5. Concluding remarks**

This paper examined the mean-reversion property of the real interest rates from a number of industrialized and East Asian countries. Most of the previous studies have found the real interest rates to be non-stationary and mean-averting. This is a puzzling outcome since the real interest rate is expected to be stationary or mean-reverting over time. We note that these past studies used the unit root testing and half-life estimation methods which are univariate in nature, totally ignoring the presence of cross-sectional dependence among the real interest rates. Distinct from the past studies, we have used panel unit root tests and half-life estimation which take explicit account of cross-sectional dependence among the real interest rates. We have employed subsampling panel unit root tests Choi and Chue (2007) and estimated the half-life of real interest rates using the vector autoregressive models. The latter is based on the bias-corrected bootstrap HDR method, which is an extension of the univariate method recently proposed by Kim et al. (2007).

The major finding of the paper is that real interest rates are overall mean-reverting and stationary for both industrialized and East Asian countries. We also have found a strong tendency that the real interest rates of more matured and liberalized capital markets show slower rate of mean-reversion than those of East Asian markets. In addition, mean-reversion of real interest rates for East Asian emerging markets has become substantially slower after the Asian crisis. We suggest that government intervention in capital control causes financial frictions which prevent

market forces from exerting full effects on the real interest rates. The rates deviate in a narrower range and revert to the long-run value at a faster rate in the presence of such friction. We note that this point needs a further investigation in a future research.

**Table 1: Unit Root Test Results for Rapach and Wohar data**

	Test Statistic	5% Subsampling Critical Values	
		MV	SC
IPS	-2.62	-2.43	-2.28
Inverse Normal	-6.53	-5.24	-5.49

MV: minimum volatility rule for subsample length selection  
 SC: stochastic calibration rule for subsample length selection

**Table 2: Unit Root Test Results for East Asian data**

	Test Statistic	5% Subsampling Critical Values	
		MV	SC
Period I			
IPS	-3.54	-2.67	-2.46
Inverse Normal	-5.02	-4.34	-4.92
Period II			
IPS	-3.17	-2.70	-2.41
Inverse Normal	-5.23	-4.29	-4.91

MV: minimum volatility rule for subsample length selection  
 SC: stochastic calibration rule for subsample length selection  
 Period I: 1987:01 to 1996:12; Period II: 1999:01 to 2007:05

**Table 3: Half-Life Estimates for Rapach and Wohar data (in years)**

	Point		95% Interval			
	RW	HDR	RW		HDR	
Australia	4.29	1.24	2.08	$\infty$	0.52	29.33
Belgium	4.38	1.12	2.49	$\infty$	0.45	6.90
Canada	3.18	0.52	1.56	$\infty$	0.30	1.16
Denmark	0.92	0.50	0.88	$\infty$	0.32	0.95
France	8.73	2.00	4.43	$\infty$	0.87	17.87
Ireland	3.11	0.38	1.42	$\infty$	0.20	0.75
Italy	4.15	0.70	1.60	$\infty$	0.33	2.35
Netherlands	0.99	0.67	0.93	$\infty$	0.37	1.38
New Zealand	4.57	1.01	1.57	$\infty$	0.45	2.65
Norway	3.86	0.67	1.28	$\infty$	0.29	1.79
Switzerland	1.52	1.95	1.19	$\infty$	0.62	8.15
UK	2.36	0.60	1.51	$\infty$	0.38	0.92
US	3.04	1.31	2.45	$\infty$	0.67	20.50
Mean	3.47	0.97	1.80	$\infty$	0.44	7.28

RW: the grid bootstrap estimates of Rapach and Wohar (2004)

HDR: Bias-corrected HDR Bootstrap estimates

**Table 4: Half-Life Estimates for East Asian Markets (in years)**

	Period I			Period II		
	Point	95% Interval		Point	95% Interval	
JPN	0.92	0.24	9.27	0.30	0.12	0.99
KOR	0.31	0.13	1.24	0.32	0.14	5.00
SNG	0.31	0.14	1.72	0.31	0.11	1.56
IND	0.16	0.09	0.43	0.12	0.08	0.16
MAL	0.57	0.18	3.83	0.24	0.10	1.46
PHP	0.07	0.05	0.10	0.48	0.17	3.12
THI	0.15	0.08	0.27	0.99	0.25	7.94
Mean	0.36	0.13	2.41	0.39	0.14	2.89
Mean*	0.25	0.11	1.18	0.43	0.15	3.54

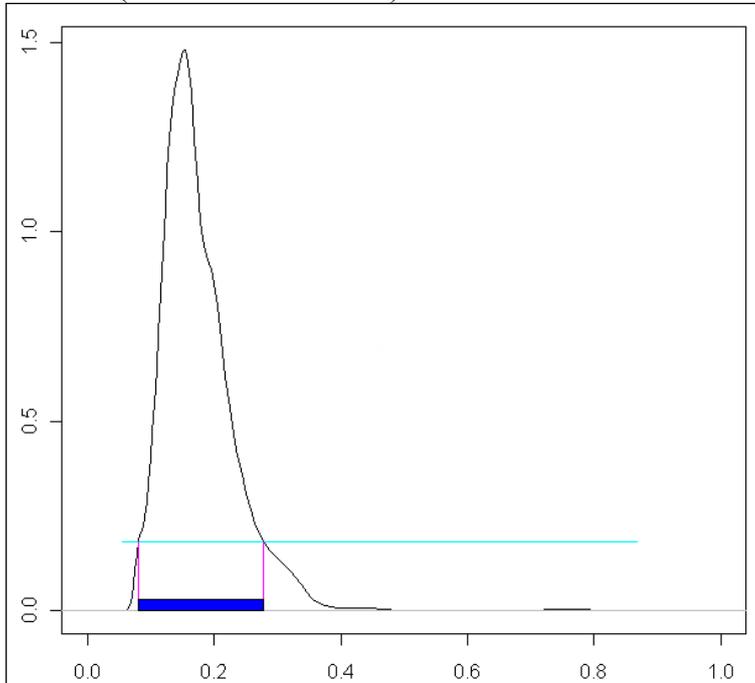
Period I: 1987:01 to 1996:12; Period II: 1999:01 to 2007:05

The entries are bias-corrected bootstrap HDR estimates

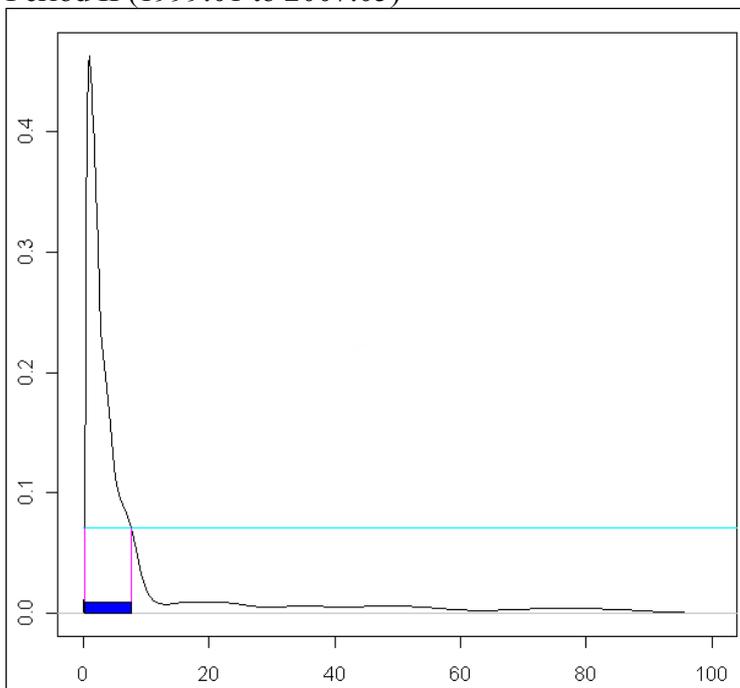
Mean indicates the average for all countries, while Mean\* indicates the average excluding Japan and Singapore

Figure 1: Density Estimates for the Bias-Corrected Bootstrap Replicates of Half-Life: the case of Thailand

Period I (1987:01 – 1996M12)



Period II (1999:01 to 2007:05)



The X-axes of both graphs indicate half-life in years

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